

## Exercises:

① Compute  $f_x$  &  $f_y$

a.  $f(x,y) = \frac{y}{x+y}$

b.  $f(x,y) = \ln(x^2+xy)$

c.  $f(x,y) = \sin x \cdot \cos y$

② 15.3 #10 :> textbook

③ For  $f(x,y) = 3x^2y + 4x^3y^2 - 7xy^5$ ,  $f_x(1,2)$

④ For  $g(x,y) = xy / (x-y)$   $g_{xy}(1,0)$

⑤ Challenge, but a good one to try:

$$f(x,y,u,v) = \frac{x^2 + e^y v}{3y^2 + \ln(2+u^2)}$$

Show  $f_{uv}xyuv = 0$

Hint: Choose a different order

⑥ Compute the gradient

a.  $f(x,y) = \cos(x^2+y)$

b.  $h(x,y,z) = xy z^{-3}$

7) Compute directional derivative of  $f$  in dir. specified by  $v$ , at the point  $P$

a.  $f(x,y) = x^2 + y^3$ ,  $v = \langle 4, 3 \rangle$ ,  $P = (1, 2)$

b.  $f(x,y) = x^2y^3$ ,  $v = i + j$ ,  $P = (1/6, 3)$

c.  $g(x,y,z) = x \ln(y+z)$ ,  $v = 2i - j + k$ ,  $P = (2, e, e)$